# Finite Element Analysis of Deformation Behavior of Wire Cold Flat Rolling 

Dr. Abdul Kareem Flaih Hassan*

Received on: 24 /10/ 2010
Accepted on: 5/5/ 2011


#### Abstract

Flat rolling of wire is an industrial process used to manufacture electrical flat wire, medical catheters, springs and piston segments, among other products. This paper presents a 3D finite element analysis of wire flat rolling. The variations of rolling force due to roll speed changes, Effect of reduction in height on width of contact Area, and Lateral spread of wire has been discussed. It is found that a negligible increase in flow stress and rolling force does occur due to increase in the strain rate at room temperature. Besides, the results showed that the behavior of rolling force variation versus roll speed depends on the rolling reductions. A theoretical relationship has been developed to relate the reduction in height of wire to the width of contact area between the rolls and wire. This relationship depicts that the width of contact area is proportional to square root of reduction in height of wire. Finally the finite element can give a reasonable estimation of the deformation behavior in wire flat rolling, since the theoretical predictions are reasonable agreement with the experimental measurements of other authors.


Keywords: wire flat rolling, wire cold rolling


$$
\begin{aligned}
& \text { الخلاصة }
\end{aligned}
$$

صناعة النوابظ واجز اء المكبس ـ هذا العمل يقدم تحليـل ثلاتي الابعـاد باستخدام طريقـة العناصر المحددة
درجـة حرارة الغرفـة. إضـافةً إلـى ذلك، لـوحظ ان قوةِ الدرفلـة عنـد سـر ع درفلـة مختلفـة يَعَتمـُ علـى مقدار
التخفيض في الارتفاع. تم اسنتباط علاقة رياضية نظرية تفسر العلاقة بين مقدار التخفيض في قطر السـلك
يتناسب طرديا" مع الجذر التربيعي للتخفيض في ارتفاع السلك. بينت النتائج المسنتبطة من نظريـة العناصر
المحددة ان هناللك تو افق مقبول في تخمـين سـلوك التشـوة لعمليـة درفلـة الاسـلاك مقارنــة هـع نتـائج عمليـة
لباحثين اخرين.
كلمـات مرشدة: درفلة المستوية للاسلاك ، درفلة الاسلاك على البارد

## College of Engineering,University of Basrah/Basrah

## 1. Introduction

The rolling process is one of the most popular processes in manufacturing industries in that almost $80 \%$ of metallic equipment has been exposed to rolling, at least one time in their production period. Among all kinds of the rolling processes, the flat rolling is the most practical one. In industrial countries, about $40-60 \%$ of rolling products are produced with this type of rolling. Therefore, many scientists have tried to enhance the quality and quantity of products by optimizing this process and identifying parameters affecting it to satisfy their customers. Flattened wires are widely used in saw blades, spring, piston rings and transformer industries. These wires are produced by the process of flat rolling, see Fig.(1). In this process, wire of circular cross section is cold rolled between two flat rolls in one or several passes to achieve the desired thickness to width ratio [1]. Finite element models have been used to analyze a number of metal-forming processes [2]. However, few models have been developed to simulate flat roll-forming processes. These processes present many computational challenges to finite element analysis. One difficulty is that full-length die contours must be modeled since the stressed area of the die changes as the forming operation progresses. Another difficulty is that nodal coordinates must be updated constantly because the blanks rotate and translate at the same time. Additionally, friction and slippage between the dies and the workpiece must be considered.

Finally, very high mesh densities are required because of the massive threedimensional material flow in the blanks.
These flat rolling characteristics increase the number of calculations at each step of the simulation.

An empirical formula for determining spread in flat rolling process was proposed and applied by Wusatowki[3], Based on Wusatowski's work, Mauk[4] has proposed the iteration method, and Bursal et al.[5] have used the vertical slab method for analysis. More general empirical formulas for various rolling shapes were proposed by Saito et al. $[6,7]$ and Shinokura and Takai $[8,9]$ by combining the experimental results shape rolling and spread formula for flat rolling.
The flat rolling of wire combines the problems of lateral spread and anisotropy. The old empirical methods used to hot rolling of shapes cannot be used to predict the spread. The single option is to use 3D finite elements with an anisotropic material formulation. As a means of controlling the accuracy of the program, experimental flat rolling can be carried out and the results compared to the FE predictions[10].

## 2. Theoretical Background

### 2.1 Width of Contact Area Between the Rolls and Wire

To achieve a relation between the width of contact area, i.e. $b$ value in Fig.1, and the reduction in height of wire, the deformation pattern during flat rolling of wire is considered. The reduction in height of wire, $\Delta \mathrm{h}$, defined as

$$
\begin{equation*}
\Delta h=d_{o}-h_{1}=h_{o}-h_{1} \ldots \tag{1}
\end{equation*}
$$

where $d_{0}\left(=h_{0}\right)$, and $h_{1}$ are the initial diameter of wire and the final height of the flattened wire, respectively. In side pressing test of rod, macroscopic shear bands are produced by the formation of two dead metal zones due to the existence of friction between the tools and wire [11]. It has been reported that the shear bands are observed in metallographic cross-section of rods and their morphology follows the reduction in height of rods, as shown in Fig. (2) b and c.

The shear bands are in an X form as shown in the figure. These bands may be considered as the slip line in side pressing test [12]. It has been ascertained that with increasing the reduction in height, the legs of the X rotate away from the primary compression axis[11,13]. From the FEM results presented by Iankov[14] and Pesin et al. [15] for the wire flat rolling process, one may conclude that after flat rolling the wire, there are two bands of X form in cross-section of wire with extremely difference in deformation with respect to the other area. Using the idea of rotation of X legs with increasing the reduction in height of wire, the width of contact area between the wire and rolls in wire flat rolling process can be calculated. Regarding to this point, the $b$ value can be calculated by the following relation in region ABC of Fig.(2) b $[16,17]$ :

$$
\begin{align*}
& \frac{b^{2}}{4}+\frac{h_{1}^{2}}{4}=\frac{h_{o}^{2}}{4}  \tag{2}\\
& b=\sqrt{h_{o}^{2}-h_{1}^{2}}=\sqrt{\Delta h\left(h_{o}+h_{1}\right)}  \tag{3}\\
& b=\sqrt{\Delta h\left(2 h_{o}-\Delta h\right)} \quad \ldots \tag{4}
\end{align*}
$$

Actually, the length of bands is slightly increased. If it is assumed that the increase is equal to $\Delta \mathrm{h} / 2$, Eq. (4) can be written as:
$b=\sqrt{2 h_{o} \Delta h} \ldots$ (5)

### 2.2 Lateral Spread of Wire in Wire Flat Rolling

Another important parameter in wire flat rolling process is the lateral spread of the wire. An approach reported for the spread in strip rolling is as follows [18]:
The mean vertical stress between the rolls and strip can be regarded as the normal pressure ( $s$ ), corresponding to a lateral compressive stress of $m s$, where $m$ is a function of the geometry of the plastic zone, rolling temperature and composition [6]. The value of $m$ lies between that of plane strain and plane stress deformation condition, i.e. $0 \leq m \leq 1 / 2$. Neglecting the stress in the longitudinal direction, then from the Levy-Mises plastic stress-strain relations, we get [18]
$\frac{d \varepsilon_{2}}{-d \varepsilon_{3}}=\frac{1-2 m}{2-m}=p \quad 0 \leq p \leq \frac{1}{2}$
$\frac{\ln \left(\frac{W_{1}}{W_{o}}\right)}{\ln \left(\frac{h_{o}}{h_{1}}\right)}=p \quad$ or $\quad \frac{W_{1}}{W_{o}}=\left(\frac{h_{o}}{h_{1}}\right)^{p} \ldots$
where $d \varepsilon_{2}$ and $d \varepsilon_{3}$ are the strains in width and height and $\mathrm{W}_{0}, \mathrm{~W}_{1}, \mathrm{~h}_{0}$ and $h_{1}$ are the initial width, final width, initial height and final height of strip, respectively.

Using the experimental results, Wusatowski has suggested the
following relationship for the spread in strip rolling process [18,19]:
$\frac{W_{1}}{W_{2}}=a^{\prime} b^{\prime} c^{\prime} d^{\prime}\left(\frac{h_{o}}{h_{1}}\right)^{p} \ldots$
where p is a function of the roll diameter and ratio of initial width to height of strip. Also, $a^{\prime}, b^{\prime}, c^{\prime}$, and $d^{\prime} \quad$ are correction factors, slightly different from unity, which allow for the variation in steel composition, rolling temperature, rolling speed and roll material, respectively [18]. It is interesting to note that Eq.(7) is similar to Eq.(8) derived from the experimental results. The difference between these relationships is due to the existence of stress in the longitudinal direction. To develop spread formula for flat rolling of wire one may modify Eq.(8) by assuming that $\mathrm{W}_{0}=\mathrm{h}_{0}=\mathrm{d}_{0}$, where $\mathrm{d}_{0}$ is the initial diameter of wire. At each deformation condition, $h_{1}, b$, and $W_{1}$, shown in Fig.(1), were calculated. Thus, using the calculated values, the graphs of $\mathrm{W}_{1} / \mathrm{W}_{0}$ versus $h_{0} / h_{1}$ were plotted at different roll speeds.

## 3. Finite Element Modeling

In this research the code DEFORM3D V6.1 was used to perform finite element analysis of wire flat-rolling process. This software is specifically designed to analyze bulk plastic deformation, and is especially suited for the present analysis. It takes advantage of the fact that plastic deformation is usually highly localized. It assigns rigid elements to the regions of the part that are not deforming, thereby reducing the number of calculations performed at each step of the simulation [20]. It also updates nodal coordinates using a
higher order scheme. This special algorithm accurately takes into account the rotation of the object when calculating new location of the rolled part. Details of this code are well established and have been reported elsewhere [21-24].

A 3D finite element rolling model has been constructed to simulate a single pass of the wire flat rolling process, see Fig.(3).High carbon steel wires of 5.5 mm diameter were used as the simulated material in this work. The rolling parameters are shown in Table (1). At each deformation condition the rolling force and geometrical characteristics of the flat wires i.e. $h_{1}, W_{1}$, and b were numerically estimated by the finite element code, see

Figure(4). The rolling reduction in height was defined as $2 r_{o}-h_{1}$, where $r_{o}$ and $h_{1}$ are the radius of initial wire and the final height of flat wire, respectively.

## 4. Results and Discussion

To validate the predicted results obtained from the constructed finite element model, it is necessary to compare these results with experimentally measured data. The experimental data of Kazeminzhad and Taheri [1] were chosen to achieve this validation. The validation of the predicted results can be arranged in the following manner.

### 4.1 Variations of Rolling Force Due to Roll Speed Changes

Fig.(5) shows the effect of rolling speed on the rolling force at different percentage reduction in height. It is clear that increasing the rolling reduction, increases the rolling force. This can be attributed to the increase in redundant work due to large plastic
deformation accompanied with high reduction. Moreover in some ranges of rolling speed, the rolling force decrease while in the other ranges it increases. Rowe [25] reported that by increasing the roll speed, the redundant work increases near the surface of the workpiece. Regarding this point, increasing the roll speed can increases the rolling force. Zhang and Lenard [26] noticed that by increasing the roll force, the coefficient of friction between the wire and rolls decreases resulting in reduction of friction work, it is, therefore, concluded that by increasing the roll speed, the rolling force are decreases. Fig.(6) shows the effect of roll speed on the strain rate at constant percentage reduction in height $\Delta h=10.9 \%$ at room temperature. It can be seen that increasing the roll speed will increases the strain rate, while roll speed has a negligible effect on the flow stress as the strain rate sensitivity exponent for high carbon steel at room temperature is very small.

### 4.2 Effect of Reduction in Height on Width of Contact Area

The variations of final width of contact area, b , versus the reduction in height at roll speed $V=42.5 \mathrm{rpm}$ are shown in Fig.(7). $\Delta r$ represents the value of deformation which happens in the radius of wire during rolling and can be calculated using the relation. $\Delta r=\left(2 r_{o}-h_{1}\right) / 2$. Kazeminzhad and Taheri[1] proposed an empirical relationship between $b$ and $\Delta r$ denoted by. $b=5.64 \sqrt{\Delta r}$. The relationship between $b$ and, $\Delta r$ derived from the results of finite element prediction, show that there is a
good agreement with empirical relationship. Also it is observed that the $b$ value is proportional to the square root of reduction in height of wire. This result is consistent with the results presented by Pater and Weronski $[12,17]$ for the width of contact area in cross-wedge rolling and rotational compression of rod.

### 4.3 Lateral Spread of Wire

The graph relating $W_{1} / W_{o}$ to $h_{o} / h_{1}$ at a roll speed of 42.5 rpm was shown in Fig.(8). As can be seen from the figure, increasing $h_{o} / h_{1}$, the magnitude of $W_{1} / W_{o}$ is increased and the following relationship can be derived 5.

## Conclusions

1. The finite element method can give a good agreement for the prediction of deformation behavior in wire flat rolling using
2. A negligible increase in flow stress and rolling force does occur due to increase in the strain rate at room temperature.
3. The behavior of rolling force variation versus roll speed depends on the rolling reductions.
4. During the deformation of flat wire rolling, the $b$ value is proportional to the square root of reduction in height of wire.

## 6. References

[1] M. Kazeminezhad, A. Karimi Taheri, "An experimental investigation on the deformation behavior during wire flat rolling process", Journal of Materials Processing Technology, 160, 2005, 313-320.
[2] J. Chakrabarty, " Applied Plasticity", Springer, New York,
[3] Z. Wusatowski, " Fundamentals of Rolling", Pergamon Press, New York, 1969
[4] P.J. Mauk, " Computer-aided roll pass design", Doctoral Dissertation, Technical University of Aachen, Aachen, Germany, 1983.
[5] F. Bursal, K. Sevenler, P. S. raghupathi, " Computer-aided analysis of metal flow in the rolling of rods and structural profiles". Int. J. Mach. Tool. Manu., 28 , 1988, pp 475-482.
[6] Y. Saito, Y. Takahashi, K. Kato, " Calculation of spread, elongation, effective roll radius, roll force and torque when rolling in the squarediamond, square-oval, and round-oval passes", J. Iron Steel Inst., Japan, 2, 1983, 1070-1077.
[7] Y. Saito, Y. Takahashi, M. Moriga, K. Kato " A new method for calculating deformation and force parameters in steel rod rolling and its application to roll pass design", J. Jpn. Soc. Technol. Plas. 24, 1983, 10701077.
[8] T. Shinokura, K. Takai," A new method for calculating spread in rod rolling", J. Applied metal working, 2, 1982, 147-160.
[9] T. Shinokura, K. Takai," Mathematical models of roll force and torque in steel bar rolling", J. Iron Steel Inst., 14, 1986, 58-64.
[10] Bjorn Carlsson, " The contact pressure distribution in flat rolling of wire", Journal of Materials Processing Technology, 73, 1998, 1-6.
[11] Semiatin SL. Jonas JJ., "Formability and workability of metals: Plastic instability and flow localization", USA, ASTM 1984.

2000, p. 651.
[12] Pater Zb, Weronski W.," Determination of the contact area between the rolling tools and the workpiece in cross rolling process", J. Mater Process Technol., 1994;45:105-110.
[13] Shahan A. R., Karimi Taheri A., " Adiabatic shear bands in titanium and titanium alloys", Materials and Design, 1993; 14(4), 243-250.
[14] Iankov R., " Finite element simulation of profile rolling of wire", J. Mater. Process. Technol., 2003; 142; 355-361.
[15] Pesin A., Salganik V., Trahtengertz E., Chemiahovsky M., Rudakov V., "Mathematical modeling of the stressstrain state in asymmetric flattening of metal band" , J. Mater Process. Technol., 2002; 125-126;689-694.
[16] M. Kazeminezhad, A. Karimi Taheri, "A theoretical and experimental investigation on wire flat rolling process using deformation pattern", Journal of Materials and Design 26 (2005) 99-103.
[17] Pater Zb. "Analysis of plane-strain rotational compression of rod by FEM", J., Mater Process Technol., 1996;60:549-554.
[18] Chitkara NR, Johnson W., "Some experimental results concerning spread in the rolling of lead", ASME J. Basic Eng 1966(June):489-499.
[19] Helmi A., Alexander J.M,."Geometric factors affecting spread in hot flat rolling of steel", J. Iron Steel Inst. 1968:1110-1117.
[20] J.T. Jinn, " DEFORM Users Group Meeting Presentation, Scientific Forming Technologies Corporation", Columbus, OH, May 2002.

[^0]Table (1): Rolling Reduction, Speeds, and Rolling Parameters Used in this Study

| $\mathrm{h}_{\mathrm{o}}$ <br> $(\mathrm{mm})$ | $\mathrm{h}_{1}$ <br> $(\mathrm{~mm})$ | Reduction (\%) <br> $\left(\mathrm{h}_{\mathrm{o}}-\mathrm{h}_{1}\right) / \mathrm{h}_{\mathrm{o}}$ | Roll speed <br> $(\mathrm{rpm})$ |
| :--- | :--- | :--- | :--- |
| 5.5 | 4.9005 | 10.9 | $42.5,50,60,69.5,81$ |
| 5.5 | 4.4220 | 19.6 | $42.5,50,60,69.5,81$ |
| 5.5 | 3.9435 | 28.3 | $42.5,50,60,69.5,81$ |
| 5.5 | 3.4815 | 36.7 | $42.5,50,60,69.5,81$ |
| 5.5 | 3.0250 | 45 | $42.5,50,60,69.5,81$ |
| Roll diameter $=150 \mathrm{~mm}$ <br> Roll width $=200 \mathrm{~mm}$ <br> Rolling temperature $=20{ }^{\circ} \mathrm{Cd}$ |  |  |  |
|  |  |  |  |



Figure (1): Sketch Showing the Process of Flat Rolling[1]


Figure (2):Schematic Illustration of the Effect of Reduction in Height of Wire.[15]


Figure (3): (a) 3D Finite Element Model (b) Meshed Wire


Figure(4) Numerically Measured Geometrical Characteristics of the Flat Wires. $h_{1}, W_{1}$, and b.
a. Wire before Rolling
b. Wire after Rolling
c. Geometry before Rolling
d. Geometry after Rolling


Figure (6) Effect of Roll Speed on the Effective Strain Rate at $\Delta \mathrm{h}=\mathbf{1 0 . 9 \%}$


Fig.(7) Dependance of the Width of Contact Area after Rolling on $\Delta r$


Fig.(8)Dependance of W 1/Wo on ho/h1


Fig.(9)Dependance of $\operatorname{In}(W 1 / W o)$ on Wo/(RDh)1/2


[^0]:    [21] S.I. Oh, W. Wu, J. Tang, A. Vedhanayagam," Capabilities and applications of the FEM code Deform: the perspective of the developer", Journal of Materials Processing Technology, 1991, 25-42.
    [22] W.T. Wu, G. Li, A. Arvind, J.P. Tang, " Development of a three dimensional finite element method based process simulation tool for the metal forming industry", Proceedings of the 1996 European Conference on Engineering Systems Design and Analysis, vol.3, PD-vol. 75, American Society of Mechanical Engineers, New York, 1996, pp. 143-150.
    [23] W. T. Wu, S. I. Oh," ALPIDT: a general purpose FEM code for simulation of non-isothermal forming processes", Transactions of the North American SME XIII Manufacturing Research Conference, vol. 13, May 1985, pp. 449-455.
    [24] W.T. Wu, S.I. Oh, T. Altan, R.A. Miller, " Automated mesh generation for forming simulation", Computers in Engineering 1990, Proceedings of the 1990 ASME International Computers in Engineering Conference, American Society of Mechanical Engineers, New York, 1990, pp. 507-515.
    [25] G.W. Rowe, "An Introduction to the Principles of Metalworking", Edward Arnold, 1965.
    [26] S. Zhang, J.G. Lenard, " The effect of the reduction, speed and lubrication viscosity on friction cold rolling", J. Mater. Process. Technol., 30, 1992, 197-210.

